**1.****INTRODUCTION**

Solar energy is more abundant during summer than in winter. The total solar energy supply is sufficient to answer the total demand of energy in dwellings. However, in order to be able to rely completely on sustainable energy sources an efficient method to store energy is required. One of the oldest and simplest way to store thermal energy is in water, for example by using a boiler. For short timeslots this is an efficient and cheap way to store heat [4]. A disadvantage is that a large volume of water is needed and that in spite of insulation, heat will be lost. Thermal storage technologies suitable for building applications are classified in three methods based on the storage principle used: sensible heat (e.g. water tanks, underground storage) [9–11], latent heat (e.g. ice, phase change materials) [12–14], and thermochemical heat storage [1]. The later heat storage method makes use of a reversible physical or chemical reaction and has higher energy storage density and almost no heat loss, compared to the two other heat storage methods [2]. One promising possibility to store thermal energy is by means of reversible gas solid reactions [8]. Heat is stored into an endothermal dissociation reaction, splitting the thermochemical material into two components (charging), and, at a later time, the energy can be retrieved from the reverse exothermal reaction between the two components (discharging) according to the reaction. An interesting storage material should be low cost, non-toxic, non-corrosive and stable with high energy storage density [3]. These requirements are fulfilled by a number of salt hydrates. In phase change materials (PCMs) heat can be stored by using a phase transition in the material. PCMs have a larger storage capacity than water [5]. A disadvantage is that phase change materials are expensive and still suffer from heat loss during storage, as storage needs to take place at temperature levels that prevent the phase change. In thermochemical materials (TCMs) heat is stored by performing a chemical reaction. TCMs have a large storage capacity and therefore they only require a small volume to store a large amount of heat. As the heat is stored by performing a chemical reaction, there is no loss of heat during storage. The storage volumes required for the annual thermal energy demand of an average household stored in water, PCM and TCM are given by [6]. The most commonly used TCMs are salt hydrates in which thermal energy is stored by drying the salt hydrate and storing the dry salt and the water separately. The reversible reaction of hydration and dehydration of a salt hydrate is shown in Eq. 1.

(1)

The interaction between salt hydrate and water progressively weakens with increasing temperature due to the reduction in the enthalpy of hydrogen bond and finally, above the lower critical solution temperature (LCST), phase separation occurs [4]. To understand and optimize the phase behavior, thermodynamic properties of aqueous solutions of Salt hydrates need to be quantified. This requires both the accurate experimental data and a good model which allows prediction of properties of the system in the range of temperature and composition in which experimental data are not available.

A large number of experimental studies have been reported in the literature on the thermodynamic properties of various salt hydrates [16] These include activity of water in the solution, phase separation behavior and solubility analysis. The data obtained from these studies are well documented by [17].The most widely used methods for activity measurements are vapor pressure osmometry [6], laser-light scattering [7], isopiestic method [7,8], dew point method [9], and sedimentation technique [10].

Regarding the phase separation studies, the coexistence curves for salt hydrates are obtained from the cloud-point data. The cloud point is measured by using either thermos-optical analysis method [11,12] or through visual observations [13–15]. Several models have been used for predicting the behavior of salt hydrates viz. those based on the osmotic virial expansion [7], those based on equations of state [16,17], the group contribution schemes [18], and those based on the lattice mean field theory [11,14–16,19–24]. Among these models, those based on the mean field theory are most widely used. Two types of mean field models are reported. The first is the modified form of the Flory-Huggins theory [11,14–16,19]. A good thermodynamic model should be able to relate the activity of salt hydrate at low temperatures with its phase behavior at high temperatures. Unfortunately, models described above use two separate sets of parameters, one to correlate the low-temperature activity data for salt hydrate and the other to correlate the phase separation data. The parameters obtained from the activity data in the low-temperature range (278–343K) are not suitable to predict LCST and the coexistence curve of salt hydrate systems. This failure stems from inaccuracies in either the model or the experimental data. A very high accuracy of the low-temperature activity data is needed since the data need to be extrapolated over a wide interval of the temperature beyond the range of the measurement and small inaccuracies in the parameter estimates are magnified. Same can be said about the inaccuracies in the model. The task is made difficult by the fact that each activity measurement technique has a relatively narrow range of temperature over which it is accurate. The data obtained using two or more technique needs to be combined in order to extend the range of temperature. This procedure is also a source of error.

Pitzer's seminal work on the ion interaction model, along with its evolved forms like Pitzer–Simonson–Clegg (PSC), serves as the cornerstone for comprehending electrolyte solutions [29, 30]. These models offer critical insights into electrolyte behavior, particularly in techniques like ion-selective electrodes and pH measurements. They meticulously describe the thermodynamic properties of electrolyte solutions, encompassing activity coefficients and osmotic coefficients, pivotal for accurate data interpretation. Moreover, these models furnish a theoretical framework to predict electrolyte behaviors under diverse conditions, thus facilitating the optimization of processes such as chemical reactions, separations, and electrochemical systems. Overall, the development and enhancement of Pitzer's model and its derivatives have profoundly deepened our understanding of electrolyte solutions and their multifarious applications.

Khoshkbarchi, Vera, Pazuki, and Sadowski have significantly enriched our comprehension of ternary systems, exemplified by the (NaCl + I- + proline + water) system, through diverse models and theories [31-33]. Their research elucidates thermodynamic properties across varying concentrations and temperatures, laying the groundwork for further exploration in this domain. Key properties discussed include activity coefficients, solubility, phase equilibria, and excess properties such as enthalpy and Gibbs energy. These insights play a pivotal role in the design and optimization of processes involving ternary systems, encompassing crystallization, extraction, and separation processes.

Utilizing the Modified Pitzer (MP) model, researchers aim to determine activity coefficients, osmotic coefficients, excess Gibbs energy, and water activity, thereby offering a comprehensive understanding of interactions within ternary systems involving electrolytes, amino acids, and water across a broad concentration and temperature range [34, 35]. The interactions discussed primarily entail ion-ion, ion-solute, solute-solute, and solute-solvent interactions, crucial for predicting thermodynamic properties and phase behavior. This research trajectory extends to investigating the thermodynamic properties of multicomponent aqueous solutions pertinent to environmental contexts. A comprehensive thermodynamic model is proposed to forecast the behavior of aqueous mixtures containing ions such as Na+, K+, Ca2+, Mg2+, Cl−, and NO3- [28].

Trausel et al. (2014) present compelling evidence that magnesium chloride (MgCl2), sodium sulfide (Na2S), calcium chloride (CaCl2), and magnesium sulfate (MgSO4) exhibit remarkable potential for thermochemical storage due to their impressive volumetric energy densities. However, further investigation into the properties of salt hydrates is imperative to ensure informed material selection, tailored to diverse operating conditions and requirements. Crucial insights into operational parameters are provided by Clausius-Clapeyron diagrams, while thermogravimetric analysis (TGA) under controlled humidity offers valuable insights into phase diagrams, with equilibrium reached more rapidly under vacuum conditions. Encapsulation using water-permeable polymers may address challenges related to the chemical and physical stability of salt hydrates. Linnow et al. (2014) contribute significantly to understanding hydration kinetics, demonstrating the high theoretical energy densities of MgSO4∙7H2O and Na2SO4∙10H2O. Piperopoulos (2020) further underscores the potential of magnesium sulfate as a storage material, especially for seasonal solar heat storage, given its exothermic hydration reaction. This research collectively propels advancements in thermochemical storage, facilitating efficient and sustainable energy utilization across diverse applications.

In the pursuit of advancing thermochemical energy storage (TCES) systems, multiple research endeavors have emerged to explore various aspects of materials, reactor design, and operational parameters. Gaeini et al. (2019) [37] focus on potassium carbonate as a thermochemical material for heat storage, meticulously investigating its de/re-hydration reactions through kinetic modeling using Thermo-Gravimetric Analysis (TGA) and Differential Scanning Calorimetry (DSC) methods. However, the exclusive concentration on potassium carbonate overlooks the potential of other materials, narrowing the scope of exploration within the field. Furthermore, the study primarily examines the behavior of potassium carbonate with water vapor, omitting crucial factors like thermal conductivity and system design, which are pivotal for real-world applicability. Similarly, Hawwash et al. (2020) [36] delve into the impact of reactor design on thermal energy storage, particularly focusing on salt hydrates. While their investigation reveals significant insights into how reactor geometry influences pressure drop, charging time, and thermochemical heat storage, the study's confinement to cylindrical and truncated cone shapes may overlook potential variations in reactor design, urging further exploration into alternative geometries for a comprehensive understanding. Desai et al. (2021) .[38] contribute a comprehensive review of TCES systems, emphasizing materials used for sorption and reaction-based TCES, along with discussions on challenges and experimental investigations. However, gaps exist, particularly regarding detailed information on certain TCES materials' safety, stability, and solubility, warranting further exploration and analysis. Conversely, Li et al. (2022) [39] provide numerical insights into the hydration process of a sorbent comprising lithium-based salt hydrate and expanded graphite in a thermal energy storage (TES) module. While offering valuable perspectives on heat and mass migration behaviors, the focus solely on numerical investigation and specific operating conditions may limit the study's ability to fully capture real-world complexities and variations. Hao et al. (2024) [40] propose a multimodule columnar packed-bed reactor for thermochemical heat storage using salt hydrates, showcasing advantages in terms of reaction rate, reaction time, and resistance loss. However, reliance on numerical simulations without experimental validation, coupled with the study's narrow focus on specific reactor design parameters, underscores the need for broader applicability considerations and validation through experimental studies.

Aforementioned salt hydrate models, focus on their application in thermochemical heat transformers (THT) for industrial waste heat recovery, energy storage, and space heating. Studies highlight salt hydrates' high energy storage density, safety, and potential for long-duration storage [41] [42]. Research emphasizes optimizing factors like thermal conductivity, porosity, and system type for efficient heat storage [43]. Kinetic studies explore dehydration/hydration rates, emphasizing the impact of temperature, pressure, particle size, and additives on reaction kinetics [44]. Composite salt hydrates show faster desorption/sorption kinetics, with diffusion being a key limiting factor. The review also discusses the classification of salt hydrate-based systems, reactor design, theoretical models, challenges, and future prospects for salt hydrate-based gas-solid thermochemical energy storage.

Utilizing correlations based on the modes, namely the generalized Flory-Huggins theory and the Extended Debye Huckel theory [18], and incorporating activity data obtained from various techniques, an attempt has been made to predict the coexistence curve for the salt hydrate systems in the LCST region. The work is presented as follows: Firstly, we describe the models governing the thermodynamics of salt hydrate systems. Then, we present the methodology used to estimate the coefficients of these models from the data on the activity of water in the salt hydrate systems. This is followed by the analysis of the results to obtain the model parameters. Finally, the selected model is utilized to grade the quality of the reported solution activity data.

**2. METHODOLOGY**

The osmotic coefficient (φ) of an aqueous electrolyte is related to the chemical potential of water, (µw), as follow:

In the given equation for the osmotic coefficient (φ), the terms have specific meanings:

µ0w is the chemical potential of water in its standard state.

Mw is the molecular mass of water.

is the number of ions produced on dissociation of one molecule of the electrolyte.

m is the molality of the electrolyte solution, R is the gas constant and T, the absolute temperature.

These variables collectively determine the extent of deviation from ideal behaviour in solutions, providing insights into the behaviour of solutes and solvents in solution dynamics.

In this work, Gibbs free energy term is given by long range (Lr) electrostatic contributions b/w ions and short range (Sr) interaction b/w all species.

Using Pitzer`s form of the Debye- Huckle (PDH) function as the electrostatic contribution to the free energy. So,

were,

nw, ns = no. of moles of water, salt respectively

vs, vw = partial molar volume (m3/mole) of salt, solvent respectively

b = the closest approach parameter

Total no. of ions per salt

Debye Huckel type constant

Where Mw = molecular weight of solvent i.e., water in gram/mol,

NA = Avogadro number,

K = Boltzmann constant, ε = permittivity of vacuum, e = electronic charge,

DS = dielectric constant of water, VS = the molar volume of water

I = the ionic strength or

The expression for the short-range interaction contribution of aqueous salt solution is obtained from Flory- Huggins theory as given below,

Where χsw = salt-water interaction parameter, which dependent on the salt concentration and temperature

and represent the moles of salt hydrate and water in salt hydrate solution, respectively. is the number of Kuhn segments in Salt hydrate chain.

The term is the generalized Flory-Huggins parameter and considered as the function of the volume fraction of the salt hydrate, , and temperature, .

is temperature dependent coefficient and as expressed as:

and are constants.

is temperature dependent coefficient are calculated using nonlinear regression method.

Derivative of Equation (4) w.r.t. moles of water and salt gives us chemical potential of water and salt hydrate respectively.

Combining equation 1 and 5 we get,

The condition for the phase equilibrium between two separate phases (Phase-1 and Phase-2) are given by,

And

By solving equation simultaneously, phase diagram can be obtained.

The critical point is given by the following conditions:

**\*THE STEPS OF MODEL IS GIVEN BRIEFLY IN SEPARATE DOCUMENT\***

**3.RESULTS AND DISCUSSION**

**3.1 REGRESSION PARAMETERS**

Table 1 – Unknown Parameters for N = 3

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
|  | **NaCl** | **LiCl** | **Li2SO4** | **MgSO4** | **CaCl2** |
| **a** | 79.25810001 | -13416.83325 | 1805.607702 | 41812.72232 | 6917.205725 |
| **b** | 0.392577746 | -13655.82569 | -1.52985731 | -1710403.759 | -2045.137046 |
| **c** | 406.7499327 | 1438.11892 | -162.818885 | -124710.7606 | -40191.75976 |
| **d** | 79.25813745 | -17830.20198 | 1804.459355 | 25437.18659 | 8303.19844 |
| **e** | 0.393322704 | 1813.197152 | -1.53831223 | -1693135.758 | -6.0165132628 |
| **f** | 406.7499327 | 1840.796406 | -314.8768451 | 114649.0606 | 38116.51935 |
| **g** | -461.7558628 | 216895.324 | -16834.84598 | -49205.42678 | -55686.377 |
| **h** | -1.299947942 | 15369.79572 | -5.859168109 | 3900142.407 | 1578.732542 |
| **i** | -2712.455354 | -25218.75124 | -5264.96013 | 5674.916688 | 7106.784597 |
| **j** | -286.6609284 | -200587.7443 | -73341.05538 | -57730.37146 | 109013.936 |
| **k** | -0.825744651 | -92.36609842 | -3.144404132 | 75602.14676 | -3999.432868 |
| **l** | -1677.795905 | 6619.358175 | 4942.140603 | 4823.346649 | -22960.88857 |

Table 2 – Unknown Parameters for N = 4

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
|  | **NaCl** | **LiCl** | **Li2SO4** | **MgSO4** | **CaCl2** |
| **a** | -0.212294839 | -8475.14118 | 1583.531513 | 735.2502247 | 8261.720861 |
| **b** | -335.4371663 | 1.951984408 | -1.523361753 | -0.791706136 | 0.574569962 |
| **c** | 10342.4994 | 11063.71503 | 335.0484774 | -175.5402835 | -2205.145069 |
| **d** | -0.207433846 | -8762.679933 | 1586.790475 | 735.2499917 | 8514.638057 |
| **e** | -323.2401916 | 1.945589229 | -1.521177232 | -0791302324 | 0.57414814 |
| **f** | -35421.30669 | -5249.227446 | 309.9047436 | -175.5427682 | 637.5750879 |
| **g** | -4.150170132 | 139528.488 | -21459.34288 | 6263.204201 | -64139.42738 |
| **h** | 357.187306 | -2.140533011 | -5.649620842 | -1.789600289 | -1.661789026 |
| **i** | 3024.992372 | -42267.20539 | -16192.5649 | -3417.892075 | 1822.071307 |
| **j** | -1.176700102 | -28829.39158 | -51230.10337 | -10121.37875 | 119035.627 |
| **k** | 9279.052789 | -3.087335404 | -3.048952414 | -1.185368643 | -1.257998805 |
| **l** | 0 | 49056.73421 | 52595.85194 | 2229.518494 | -1687.598625 |
| **m** | 102073.3323 | -139583.3918 | -4265.223202 | -1750.261638 | 5734.631344 |
| **n** | -0.353976317 | -2.475147526 | -1.159889792 | -0.569492703 | -0.617783764 |
| **o** | -33101.67039 | -35949.50214 | -78519.87037 | -6399.459638 | -28747.96172 |

**1] NaCl**

**A. PARITY PLOT GRAPHS**

**A graph of a function

Description automatically generated with medium confidence**

Fig 1. Parity plot of NaCl for N=3

**A graph of a graph

Description automatically generated with medium confidence**

Fig 2. Parity plot of NaCl for N=4

**B. PHASE DIAGRAM GRAPHS**

**A graph of a graph showing a number of numbers

Description automatically generated with medium confidence**

Liquid + NaCl

Liquid + Ice

2H2O

Fig 3. Temperature vs Volume fraction of NaCl

Fig 3. represents the phase diagram of NaCl + H2O system. The diagram shows areas that represent a particular mixture of salt of NaCl and water at a given temperature. The point at a temperature of 253K is called eutectic point, which is the lowest temperature at which a liquid phase is stable at a given pressure. It's when a solid solute, a solid solvent, and a liquid mixture all exist in the same phase. The eutectic point is also known as the eutectic temperature and is the lowest possible melting point over all of the mixing ratios of the constituents. The temperature range of 253K to 272K represents the NaCl.2H2O + liquid system which means that you have a rock salt crystal with water molecules as a kind of dissolved impurity (2H2O molecules occupying the place of one NaCl unit), whereas the temperature this represents the NaCl + liquid system. The complete solid – liquid equilibrium data is traced almost exactly with experimental values for both N=3 and N=4 lines.

**2. LiCl**

**A. PARITY PLOT GRAPHS**

A graph of a graph

Description automatically generated

Fig 4. Parity plot of LiCl for N=3

A graph of a graph of a graph

Description automatically generated with medium confidence

Fig 5. Parity plot of LiCl for N=4

**B. PHASE DIAGRAM GRAPH**

**A graph of a graph showing a number of numbers and a line

Description automatically generated with medium confidence**

Liquid + ice

Liquid + LiCl

1H2O

2H2O

3H2O

5H2O

Fig 6. Temperature vs Volume fraction of LiCl

Fig 6 represents the phase diagram for LiCl + H2O system. Besides anhydrous LiCl, there exist four solid lithium chloride hydrates, with respectively 1, 2, 3, and 5 water molecules. These salts are extremely soluble in water. For example, the solubility of the monohydrate LiCl.H2O is about 20 mol/kg of H2O in pure water at 273 K. At the eutectic temperature of the LiCl + H2O system (199 K), which is one of the lowest of all alkali + water or alkaline earth + water systems, the stable solid is the pentahydrate LiCl.5H2O. Despite this very low temperature, the concentration of the saturated solutions is very high, 24% volume fraction of salt at the eutectic. The calculated liquidus in the LiCl + H2O system showed good agreement with the experimental results for both N=3 and N=4 lines.

**3. CaCl2**

**A. PARITY PLOT GRAPHS**

**A graph of a graph

Description automatically generated**

Fig 7. Parity plot of CaCl2 for N=3

**A graph of a graph

Description automatically generated**

Fig 8. Parity plot of CaCl2 for N=4

**B. PHASE DIAGRAM GRAPH**

**A graph of a graph showing a number of data

Description automatically generated**

4H2O

2H2O

6H2O

Fig 9. Temperature vs Volume fraction of CaCl2

Fig 9 represents the phase diagram for CaCl2 + H2O system. Phases at equilibrium for the chemical system CaCl2 + H2O are shown as a function of volume fraction of CaCl2 salt and temperature. There are three solid CaCl2 hydrates of 2, 4 and 6. In which CaCl2.6H2O and CaCl2.2H2O occur naturally and have mineral names which are called as antarctictites and sinjarites respectively. The eutectic point of this system is around 223.5K. Till the volume fraction of 0.4, our model showed an excellent agreement with the experimental data for both N=3 and N=4 lines, above with N=4 line tried to trace almost with the experimental data where N=3 line showed a slight deviation till volume fraction of 0.56.

**4. Li2SO4**

**A. PARITY PLOT GRAPHS**

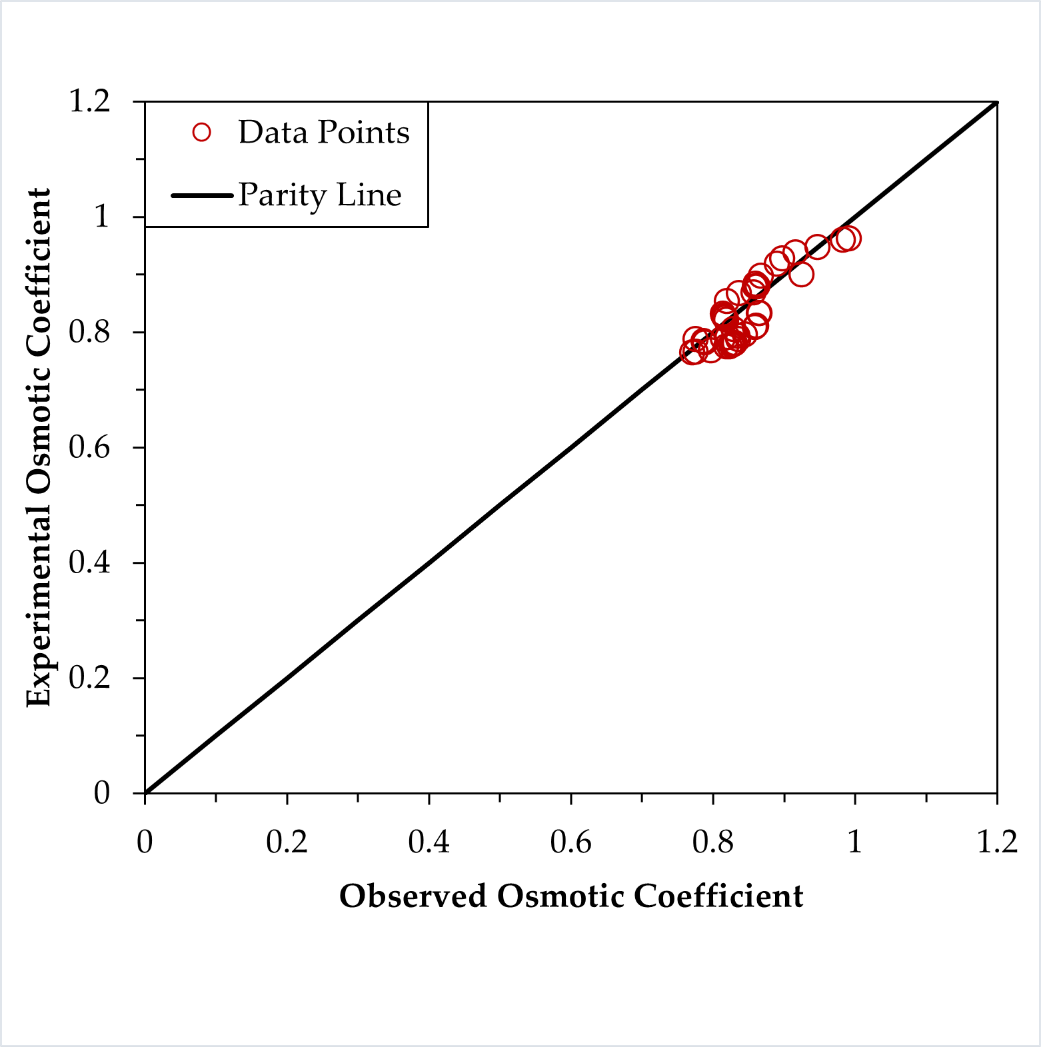


Fig 10. Parity plot of Li2SO4 for N=3

A graph of a graph with a line

Description automatically generated with medium confidence

Fig 11. Parity plot of Li2SO4 for N=4

**B. PHASE DIAGRAM GRAPH**

A graph of a graph of a graph

Description automatically generated with medium confidence

Liquid + ice

H2O

Fig 12. Temperature vs Volume fraction of Li2SO4

Fig 12. represents the phase diagram of Li2SO4 + H2O system. This system depicted a simple curve. There is a slight increase in the solubility of Li2SO4 till the eutectic point of around 250K. Here there exist only one form of hydrate salt which is Li2SO4.H2O. Our model made an excellent argument in terms of tracing the experimental values with our model values for both N=3 and N=4.

**5. MgSO4**

**A. PARITY PLOT GRAPHS**

**A graph of a graph with red circles

Description automatically generated**

Fig 13. Parity plot of MgSO4 for N=3

**A graph of a function

Description automatically generated with medium confidence**

Fig 14. Parity plot of MgSO4 for N=4

**B. PHASE DIAGRAM GRAPH**

**A graph of a graph of a graph

Description automatically generated with medium confidence**

1H2O

11H2O

6H2O

7H2O

5H2O

Fig 15. Temperature vs Volume fraction of MgSO4

Fig 15 represents the phase diagram of MgSO4 + H2O system. The phase diagram for the MgSO4 + H2O system is more complex because there are more than three phases that can exist. In addition to the solid, liquid, and gas phases, there are also several hydrate phases. Those different hydrate include a count of 1, 4, 5, 6, 7 and 11 molecules of H2O. The phase diagram for the MgSO4 + H2O system is useful for understanding the behaviour of this system in different conditions. For example, the diagram can be used to determine the conditions at which magnesium sulphate heptahydrate will form or decompose. This information can be used in a variety of applications, such as the production of magnesium sulphate and the desalination of water. Our model gave an excellent result of aligning with the experimental values for both N=3 and N=4. There is a slight deviation from the experimental values in between the volume fraction of 0.0036 till 0.011.

**4. CONCLUSION**

The model calculated phase diagrams of the Li2SO4+H2O, NaCl+ H2O, LiCl+ H2O, MgSO4+ H2O and CaCl2+ H2O systems compared with solubility data reported in literature are plotted in the above graphs. The unknown parameters of the equation 5, which helped us achieve this were tabulated in the table 1 and 2. There were 12 and 15 unknown parameters were there for n=3 and n=4 respectively. As shown in above graphs, most of the solid-liquid equilibria data, i.e. the points on the solubility curve, can be reproduced well using the present comprehensive thermodynamic models. Ice solubility data for all these systems can be accurately predicted even though they were not used in model parameterization.

For NaCl, we were able to exactly map the data against the literature work. We can be able to observe minor changes in the temperature with an increase in the volume fraction from 0.02 to 0.15, above with there is a sudden increase in the temperature from 250K till 550K. This shift indicates the reduction in the water molecules attached with NaCl from ice, NaCl.2H2O to NaCl.H2O. Similarly, our model well performed in tracing the graphs for Li2SO4 as shown in the above graphs. There was a slight deviation for CaCl2 between the volume fraction of 0.42 to 0.53, which is a region of 2 H2O molecules attached with it.

The available solubility data of MgSO4 between the volume fraction of salt hydrate from 0.10 to 0.12 and 0.16 till 0.18 are kind of scattered and hard to give a critical evaluation on their reliability. Nevertheless, the model result was not affected by the scattered experimental data significantly in those volume fraction of salt hydrate but gave a regular variation. In the system of MgSO4+ H2O, the solubilities of metastable solid phases MgSO4·4 H2O and MgSO4·5 H2O were also tried to simulate except for those stable solid phases. MgSO4·11 H2O was recognized as stable phase at low temperature, although the solid phase corresponding to its solubilities in early literature were determined as MgSO4·12 H2O.

The difference of eutectic temperature of Li2SO4· H2O +ice between the present model predicted value and that recommended by Linke [76] and Sohr et al. [75] is about 2 K. According to the critical evaluation of Sohr et al. [75], the uncertainty of the eutectic temperature is 2 K. So, in such an uncertainty range, the present model result agrees with the recent recommendation of Sohr et al. [75] well. The eutectic composition of this invariant point predicted from the present model agree with those reported by Linke [76] and Sohr et al. [75] in absolute error 0.6% weight percentage, which is in accordance with the uncertainty reported by Sohr et al. [75] recently.

The parity plot for each salt hydrates explains how well this model has predicted its output compared to the Literature data. Our model almost traced its value with the literature value and gave us the error deviation of less than 4%.

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